# GCSE Mathematics <br> <br> Practice Tests: Set 11 

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## Paper 1H (Non-calculator)

## Time: 1 hour 30 minutes

You should have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided - there may be more space than you need.

- Calculators may be used.
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must show all your working out.


## Information

- The total mark for this paper is 80
- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.


## Answer ALL questions.

## Write your answers in the spaces provided.

## You must write down all the stages in your working.

1
(a) Simplify $w^{5} \times w^{7}$
$\qquad$
(b) Simplify $t^{9} \div t^{3}$
$\qquad$

2 Solve $4 x-13=17+8 x$

$$
x=
$$

$\qquad$

3 Show that $5 \frac{2}{3}-2 \frac{3}{4}=2 \frac{11}{12}$

4 Simplify fully $\left(x^{12} y^{8}\right)^{\frac{3}{4}}$
$\mathscr{E}=\{11,12,13,14,15,16,17,18,19,20\}$
$A=\{$ even numbers $\}$
$B=\{$ multiples of 3$\}$
List the members of the set
(i) $A \cap B$
(ii) $A \cup B$

6 (a) Complete the table of values for $y=1+5 x-x^{2}$

| $x$ | -1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ |  | 1 |  | 7 | 7 |  | 1 |  |

(b) On the grid, draw the graph of $y=1+5 x-x^{2}$ for values of $x$ from -1 to 6

(2)
(Total for Question 6 is 4 marks)
$7 \quad$ Simplify $\quad\left(5 x y^{2}\right)^{3}$

8 Expand and simplify $(x+2)(2 x+3)(x-7)$
Show your working clearly.
$9 \quad$ Line $\mathbf{L}$ is drawn on the grid.


Find an equation for $\mathbf{L}$.
(Total for Question 9 is $\mathbf{3}$ marks)

10 The histogram shows information about the ages of all the passengers travelling on a plane. No one on the plane is older than 80 years.


24 passengers on the plane are aged between 40 years and 60 years.
(a) Work out the total number of passengers on the plane.

A passenger on the plane is picked at random.
(b) Work out an estimate for the probability that this person is older than 55 years.

11 Sandeep recorded the length of time, in minutes, that each of 100 adults went for a walk one Saturday afternoon.
The cumulative frequency table gives information about these times.

| Time ( $t$ minutes) | Cumulative <br> frequency |
| :---: | :---: |
| $30<t \leq 40$ | 6 |
| $30<t \leq 50$ | 20 |
| $30<t \leq 60$ | 56 |
| $30<t \leq 70$ | 84 |
| $30<t \leq 80$ | 95 |
| $30<t \leq 90$ | 100 |

(a) On the grid, draw a cumulative frequency graph for the information in the table.

(2)
(b) Use your graph to find an estimate for the median length of time that these adults went for a walk.
minutes

One of the 100 adults is chosen at random.
(c) Use your graph to find an estimate for the probability that this adult went for a walk for more than 72 minutes.

12 Solve the simultaneous equations

$$
\begin{aligned}
2 x^{2}+3 y^{2} & =5 \\
y & =2 x+1
\end{aligned}
$$

Show clear algebraic working.

13 Make $m$ the subject of $p^{2}=\frac{x+m}{2 m-y}$

14 The straight line $\mathrm{L}_{1}$ has equation $2 y=6 x-5$
The straight line $\mathrm{L}_{2}$ is perpendicular to $\mathrm{L}_{1}$ and passes through the point $(9,-1)$
Find an equation for $L_{2}$
Give your answer in the form $a y+b x=c$

15 A curve has equation $y=\mathrm{f}(x)$
There is only one maximum point on the curve.
The coordinates of this maximum point are $(4,3)$
Write down the coordinates of the maximum point on the curve with equation
(i) $y=\mathrm{f}(x-5)$
(ii) $y=3 \mathrm{f}(x)$
$\qquad$
$\qquad$

The functions $f$ and $g$ are defined as

$$
\mathrm{f}(x)=\frac{x}{4 x-3} \quad \text { and } \quad \mathrm{g}(x)=x-5
$$

(a) State which value of $x$ must be excluded from any domain of the function f .
(b) Find fg $(x)$.

Simplify your answer.

$$
\mathrm{fg}(x)=
$$

$\qquad$
(c) Express the inverse function $\mathrm{f}^{-1}$ in the form $\mathrm{f}^{-1}(x)=\ldots$

$$
\mathrm{f}^{-1}(x)=
$$

$\qquad$

Part of the curve with equation $y=\mathrm{h}(x)$ is shown on the grid.

(d) Find an estimate for the gradient of the curve at the point where $x=-0.5$ Show your working clearly.

17 Given that $3^{n}=\frac{3^{x}}{9^{y}}$, find an expression for $n$ in terms of $x$ and $y$.

$$
n=
$$

(Total for Question 14 is $\mathbf{2}$ marks)

18 A box contains marbles.
4 of the marbles are red.
The rest of the marbles are yellow.
Antonia takes at random a marble from the box and does not replace it.
Sergio then takes at random a marble from the box.
The probability that Antonia and Sergio both take a yellow marble is 0.7
Work out how many marbles were originally in the box.
Show your working clearly.

19 Write $5+12 x-2 x^{2}$ in the form $a+b(x+c)^{2} \quad$ where $a, b$ and $c$ are integers.

20 Here is the graph of $y=a \sin (b x)^{\circ}$ for $0 \leq x \leq 360$


Find the value of $a$ and the value of $b$.

$$
\begin{aligned}
& a=. \\
& b=.
\end{aligned}
$$

$\qquad$
(Total for Question 20 is 2 marks)

21 The table gives information about the first six terms of a sequence of numbers.

| Term number | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Term of sequence | $\frac{1 \times 2}{2}$ | $\frac{2 \times 3}{2}$ | $\frac{3 \times 4}{2}$ | $\frac{4 \times 5}{2}$ | $\frac{5 \times 6}{2}$ | $\frac{6 \times 7}{2}$ |

Prove algebraically that the sum of any two consecutive terms of this sequence is always a square number.


Diagram NOT accurately drawn

$$
\overrightarrow{O A}=\mathbf{a} \quad \overrightarrow{O C}=\mathbf{c} \quad \overrightarrow{A B}=2 \mathbf{c}
$$

$P$ is the point on $A B$ such that $A P: P B=3: 1$
$Q$ is the point on $A C$ such that $O Q P$ is a straight line.
Use a vector method to find $A Q: Q C$
Show your working clearly.
$\qquad$

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